# University of Sri Jayewardenepura Department of Mathematics Semester I - 2017

#### MAT 455 2.0/ASP 423 2.0 Graph Theory

Lecturer-in-Charge	Lecture Room	Email	Time
Dr. G. H. Jayantha Lanel	M2	ghjlanel@sjp.ac.lk	Tue : 10.15a.m12.00noon

## Objectives

The aims of this course are twofold. First, to provide an introduction to fundamental of graph theory and graph algorithms. Second, to emphasis many examples and applications of graphs.

## **Intended Syllabus**

- 1. Graphs
  - 1.1. Basic definitions in graph theory
  - 1.2. Traveling through a graph
    - 1.2.1. Connectedness
    - 1.2.2. Euler tours
    - 1.2.3. Hamiltonian cycles
  - 1.3. Graph representation
    - 1.3.1. Adjacency matrices
    - 1.3.2. Adjacency lists
  - 1.4. Planarity of Graphs
    - 1.4.1. Euler's formula
    - 1.4.2. Kuratowski's theorem
  - 1.5. Coloring of graphs
    - 1.5.1. Vertex coloring, edge coloring, and Chromatic number
    - 1.5.2. Color theorems

## 2. Trees

- 2.1. Basic definitions for trees
  - 2.1.1. Rooted trees
  - 2.1.2. Ordered trees, binary trees, and m-ary trees
- 2.2. Spanning trees
  - 2.2.1. Depth-first search

- 2.2.2. Breadth-first search
- 2.3. Minimum spanning trees
  - 2.3.1. Prim's algorithm
  - 2.3.2. Kruskal's algorithm
- 3. Paths and Flows
  - 3.1. Shortest paths and longest paths
    - 3.1.1. Dijkstra's algorithm
    - 3.1.2. The traveling salesman problem
  - 3.2. Flows
    - 3.2.1. The Ford-Fulkerson algorithm
    - 3.2.2. The maxflow-mincut theorem

## **References**

- 1. *Graph Theory and Its Applications* by Jonathan L. Gross and Jay Yellon (available in the main library).
- 2. Handbook of Graph Theory by Jonathan L. Gross, Jay Yellon and Ping Zhang.

#### **Learning Outcomes**

On successful completion of this module, the student should be able to:

- demonstrate an understanding of the general concepts in graph theory
- apply the abstract concepts of graph theory in modeling and solving problems in different fields of study
- demonstrate the abilities in critical thinking and problem solving.

#### Assessment Criterion

Continuous Assessment	40%
End of Semester Examination	60%

## **Method of Continuous Assessment**

- 1. Assignments will be assigned frequently and will always be collected.
- 2. Unannounced quizzes will be given at the end of randomly selected lectures.
- 3. There will be a group project worth 15% of your final grade. Your group will need to choose a graph theory paper published in a journal within the last 5 years, prepare a written report on it, and present it in class.